

- (d) The off-peak period of the cherry season is followed by a peak period that lasts for 64 days. Every day during the peak period all cherries are inspected and:
- 95.2% are classified as Unripe and are left on the tree to be checked the next day
 - 4% are classified as Ripe and are picked and sold
 - 0.8% are classified as Damaged and are picked and made into jam.

(i) Write down the new transition matrix U which would apply in the peak season.

(1 mark)

ii. Determine, correct to the nearest whole number, the number of kilograms of:

a) ripe cherries

2 marks

b) damaged cherries

that will have been produced over the entire cherry season by this orchard.

1 mark

Question 2

Scientists are studying the changes in the number of female frogs living along a creek bed. The scientists have established the following information about how the female frog population changes over time.

- No female frogs live beyond the age of 3 years.
- The stages of the frogs' development are: tadpole, frogteen and adult
- Females less than a year old are immature and cannot reproduce
- Only 50% of all tadpoles reach the age of one year (when they become a frogteen)
- Frog teens produce an average of 1.2 female tadpoles in that year.
- Only 20% of frogteens reach the age of 2 (when they become adults)
- Adult frogs produce on average 2 female tadpoles in that year.

The scientists have represented this information in a matrix.

$$P = \begin{array}{ccc} & \begin{array}{c} \textit{This year} \\ T \quad F \quad A \end{array} & \\ \begin{array}{c} T \\ F \\ A \end{array} & \begin{bmatrix} 0 & 1.2 & 2 \\ 0.5 & 0 & 0 \\ 0 & 0.2 & 0 \end{bmatrix} & \begin{array}{c} T \\ F \\ A \end{array} \end{array} \quad \begin{array}{c} \\ \\ \textit{Next year} \end{array}$$

The number of tadpoles, frogteens and adults at the time of the study are represented by the matrix:

$$O = \begin{bmatrix} 200 \\ 80 \\ 20 \end{bmatrix} \begin{array}{c} T \\ F \\ A \end{array}$$

- a. Find the matrix product PO and explain what information it gives.

2 marks

- b. Determine how many adult frogs, to the nearest whole number, there will be after 5 years, according to his scientific model.

1 mark

c. Calculate decrease in the total frog population along the creek bed between year 2 and year 3. Give your answer correct to the nearest whole number.

2 marks

c. In the longrun, describe what happens to the frog population in the creek, according to this scientific model. Justify your answer with appropriate calculations

2 marks

d. If each frogteen produces on average x tadpoles (instead of 1.2) it is found that the total population of frogs remains constant at a value close to 300. Find the value of x , correct to one decimal place.

2 marks

